

A Methodology for Knowledge Acquisition by  
Heterogeneous STRIPS-Based Planners

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# Outline

- Introduction
- Problem Formulation
- Definitions
- Learning Methodology
- Detailed Example
- Related Work
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# Introduction

- We can achieve communication in a network of heterogeneous planning systems through translation
- If a problem cannot be solved,
  - it indicates a lack of knowledge within the planner
  - results in the need to send out a query to other planners
- To avoid future queries and solve other similar problems, the planner should acquire knowledge from the solutions that it receives from other planners
- The challenges
  - Many different ways to learn
  - Knowledge representation may be at different levels of abstraction
  - Preserve the correctness of the knowledge base

## Problem Formulation

# Components of the System

- *Planner<sub>i</sub>* contains
  - Knowledge Base -  $KB_i$  with
    - Predicates -  $Pred_i$
    - Actions –  $Actions_i$ 
      - $Pre(a_i^k), Add(a_i^k), Del(a_i^k), Con(a_i^k)$
    - Translators –  $Trans_i$
  - Domain Truth Table
    - Sets of predicates that can never exist together and those that cannot exist separately in the domain theory of *Planner<sub>i</sub>*
    - Predicates that are always true or always false with respect to the common ontology
- Common Ontology - the knowledge representation which used by all planners to communicate with each other.

## Problem Formulation

# Communication between Planners

- Communication is through
  - Queries containing Initial Conditions, Goals and Constraints  
 $Query_i = \langle I_i, G_i, C_i \rangle$
  - Plans containing Actions and Orderings  
 $Plan_i = \langle A_i, O_i \rangle$
- Communication occurs with the following steps
  - In Planner<sub>i</sub>
    - Create  $Query_i = \langle I_i, G_i, C_i \rangle$
    - Translate and send as  $Query_{co} = \langle I_{co}, G_{co}, C_{co} \rangle$
  - In Planner<sub>j</sub> :
    - Receive  $Query_{co}$  and translate to  $Query_j = \langle I_j, G_j, C_j \rangle$
    - Create the solution,  $Plan_j = \langle A_j, O_j \rangle$
    - Translate and send  $Plan_{co} = \langle A_{co}, O_{co} \rangle$  as the reply
  - In Planner<sub>i</sub>
    - Receive the solution and translate to  $Plan_i = \langle A_i, O_i \rangle$

## Communication between Planners

- Translation implies that equivalent knowledge is present.
- If this is not true, the solution cannot be represented in the domain theory of *Planner<sub>i</sub>*. Hence, the solution cannot be used.
- Objective – To present a methodology that will achieve translation through learning while preserving the correctness of knowledge in the domain theory of the planner.

Problem Formulation  
Formal Objective

- Given  $Plan_j = \langle A_j, O_j \rangle$  in the domain theory of  $Planner_j$  to add  $Pred_i^{new}$ ,  $Actions_i^{new}$  and  $Trans_i^{new}$  to  $KB_i = \langle Pred_i, Actions_i, Trans_i \rangle$ , in the domain theory of  $Planner_i$ , such that
  - $Plan_j = \langle A_j, O_j \rangle$  can be translated to  $Plan_i = \langle A_i, O_i \rangle$  with the following properties
    - $Plan_i \equiv Plan_j$
    - $Plan_i$  is a correct plan
    - $Plan_i$  is a solution for  $Query_i = \langle I_i, G_i, C_i \rangle$
  - Constraints on this solution
    - $Actions_i^{new}$  is minimal subject to the individual actions being the most similar to  $Actions_i$  when compared to any other  $Actions_i^{new'}$  that could have been added to  $KB_i$
    - $KB_i' = \langle Pred_i \cup Pred_i^{new}, Actions_i \cup Actions_i^{new}, Trans_i \cup Trans_i^{new} \rangle$  is consistent and all its elements are correct

## Problem Formulation

### Why is this Non-Trivial?

- Creating an algorithm for a heuristic process
- Given  $Plan_j$  with  $m$  actions, maximum number of plans  $N$  considered for learning is in the range

$$2^{m-1} < N < B_m$$

where  $B_m$  is a Bell number corresponding to the number of ways to partition a set in to non-empty subsets.

$$B_{m+1} = \sum_{k=0}^m B_k \binom{m}{k}, \text{ with } B_0 = 1$$

e.g. with  $m = 8$  actions,  $128 < N < 4140$



## Definitions - Equivalence of Knowledge

- The subset of predicates,  $Pred_i^p$  from  $Planner_i$  is equivalent to the subset of predicates,  $Pred_j^q$  in  $Planner_j$  if their aggregate semantics are the same. In this case we write  $Pred_i^p \equiv Pred_j^q$

$$Pred_i^p = Tower_i(A,B,C)$$

$$Pred_j^q = On_j(A,B), On_j(B,C), On_j(C, Table), Clear_j(A)$$

- Two plans,  $Plan_i = \langle A_i, O_i \rangle$  and  $Plan_j = \langle A_j, O_j \rangle$  are equivalent ( $Plan_i \equiv Plan_j$ ) if  $Pre(Plan_i) \equiv Pre(Plan_j)$ ,  $Add(Plan_i) \equiv Add(Plan_j)$ ,  $Del(Plan_i) \equiv Del(Plan_j)$  and  $Con(Plan_i) \equiv Con(Plan_j)$ .

$Plan_i$

$$A_i = 2\_Tower\_to\_Table_i(D,E), 3\_Tower\_to\_Tower_i(A,B,D)$$

$$O_i = before(2\_Tower\_to\_Table_i(D,E), 3\_Tower\_to\_Tower_i(A,B,D))$$

$Plan_j$

$$A_j = Unstack_j(D,E), Putdown_j(D), Unstack_j(A,B), Stack_j(A,D)$$

$$O_j = before(Unstack_j(D,E), Putdown_j(D)), before(Putdown_j(D), Unstack_j(A,B)), before(Unstack_j(A,B), Stack_j(A,D))$$

## Definitions - Correctness of Knowledge

- An action  $a_i^k$  is correct in  $Planner_i$  if
  - $Del(a_i^k)$  is a subset of  $Pre(a_i^k)$ .
  - $\nexists P_i^k \subset Pre(a_i^k)$  or  $\nexists P_i^k \subset Add(a_i^k)$  or  $\nexists P_i^k \subset Con(a_i^k)$ , such that  $P_i^k$  is listed as always false in the Domain Truth Table of  $Planner_i$
  - $\nexists P_i^k \subset Del(a_i^k)$ , such that  $P_i^k$  is listed as always true in the Domain Truth Table of  $Planner_i$
- $Plan_i = \langle A_i, O_i \rangle$ , produced by  $Planner_i$  is correct if
  - The orderings between the actions in  $Plan_i$  are acyclic.
  - All actions in  $A_i$  are correct with respect to the domain theory of  $Planner_i$
- $Plan_i = \langle A_i, O_i \rangle$  is a solution to  $Query_i = \langle I_i, G_i, C_i \rangle$  if
  - $Plan_i$  is correct plan.
  - $Pre(Plan_i)$  is a subset of  $I_i$
  - $G_i$  is a subset of  $Add(Plan_i)$
  - $C_i$  is a subset of  $Con(Plan_i)$

## Definitions – Similarity of Knowledge

- Similarity Index(*SI*) - the ratio of the number of common predicates between actions to the total number of predicates in both actions. Ranges from 1(actions are equal) to 0 (actions have no common predicates)

$$SI(a_i^p, a_i^q) = \frac{|Common\_pred(a_i^p, a_i^q)|}{|Not\_common\_pred(a_i^p, a_i^q)| + |Common\_pred(a_i^p, a_i^q)|}$$
$$SI(a_i^p, a_i^q) = 0, \text{ if } Common\_pred(a_i^p, a_i^q) = \{ \}$$

where

$$p_i^k \in Common\_pred(a_i^p, a_i^q) \text{ if } (p_i^k \in Pre(a_i^p) \wedge p_i^k \in Pre(a_i^q)) \\ \vee (p_i^k \in Add(a_i^p) \wedge p_i^k \in Add(a_i^q)) \vee (p_i^k \in Con(a_i^p) \wedge p_i^k \in Con(a_i^q)), \\ \text{otherwise } p_i^k \in Not\_common\_pred(a_i^p, a_i^q)$$

- If  $SI(a_i^p, a_i^k) > SI(a_i^q, a_i^k)$ , then action  $a_i^p$  is more similar than action  $a_i^q$  when compared to action  $a_i^k$ .

## Definitions – Similarity of Knowledge

- The Similarity Index of two sets of actions,  $A_i^p$  and  $A_i^q$ , is defined as

$$SI(A_i^p, A_i^q) = \frac{|Sum\_Similarity\_Index|}{|A_i^p|}$$

where

$$Sum\_Similarity\_Index = \sum SI(a_i^r, a_i^s), \forall a_i^r \in A_i^p \text{ and } a_i^s \in A_i^q \text{ such that,}$$
$$SI(a_i^r, a_i^s) > SI(a_i^r, a_i^m) \forall a_i^m \in A_i^q, m \neq s.$$

- If  $SI(A_i^p, A_i^k) > SI(A_i^q, A_i^k)$ , then the set of actions  $A_i^p$  is more similar than the set  $A_i^q$  when compared to the set of actions  $A_i^k$ .

## Methodology

# Learning Algorithm

1. For  $Plan_{co} = \langle A_{co}, O_{co} \rangle$ , generate all possible partitions of actions in  $A_{co}$  and corresponding orderings.

$$Partition_{co}^n = \{ \langle A_{co}^{n-1}, O_{co}^{n-1} \rangle \langle A_{co}^{n-2}, O_{co}^{n-2} \rangle \dots \langle A_{co}^{n-n}, O_{co}^{n-n} \rangle \langle O_{co}^{n-m} \rangle \}$$

2. Eliminate all partitions,  $Partition_{co}^k$ , that will result in plans which are not acyclic.

$Partition_{co}^k$  is eliminated if,  $\exists before(a_{co}^p, a_{co}^q) \in O_{co}^{k-m}$  and  $\exists before(a_{co}^r, a_{co}^s) \in O_{co}^{k-m}, p \neq q \neq r \neq s, a_{co}^p, a_{co}^s \in A_{co}^{k-x}$  and  $a_{co}^q, a_{co}^r \in A_{co}^{k-y}, x \neq y$

3. Eliminate the partitions that will result in plans containing incorrect actions.

From the remaining partitions, select those which contain the most number of elements  $\langle A_{co}^{k-l}, O_{co}^{nk-l} \rangle$  which can be translated to the domain theory of  $Planner_i$ .

## Methodology

# Learning Algorithm

4. For every *Partition*<sub>co</sub><sup>k</sup> selected above, form a set of actions  $A_i^k$  such that,  $\forall \langle A_{co}^{k-l}, O_{co}^{k-l} \rangle \in \text{Partition}_{co}^k$  that cannot be translated by *Planner*<sub>i</sub>,  $\exists a_i^l \in A_i^k, a_i^l \equiv \langle A_{co}^{k-l}, O_{co}^{k-l} \rangle$ .
- Each action  $a_i^l$  in  $A_i^k$  is formed as follows.
  - Partition  $Pre(\langle A_{co}^{k-l}, O_{co}^{k-l} \rangle)$  into  $\{P_{co}^1, P_{co}^2, \dots, P_{co}^n, P_{co}^m\}$  such that,  $\forall P_{co}^k, k=1 \dots n, \exists t_i^k \in \text{Trans}_i$  that represents the mapping

$$P_{co}^k \xleftrightarrow{t_i^k} P_i^k$$

and  $\forall p_{co}^r \in Pre(\langle A_{co}^{k-l}, O_{co}^{k-l} \rangle) \wedge p_{co}^r \notin P_{co}^k, k=1 \dots n, p_{co}^r \in P_{co}^m$   
Similarly, partition  $Add(\langle A_{co}^{k-l}, O_{co}^{k-l} \rangle)$ ,  $Del(\langle A_{co}^{k-l}, O_{co}^{k-l} \rangle)$  and  $Con(\langle A_{co}^{k-l}, O_{co}^{k-l} \rangle)$ .

- Form action  $a_i^l$  with  $Pre(a_i^l) = P_i^1 \cup P_i^2 \cup \dots \cup P_i^n \cup P_{co}^m$  where  $P_i^k$  is the translation of  $P_{co}^k$ , i.e.

$$P_{co}^k \xleftrightarrow{t_i^k} P_i^k$$

In a similar manner,  $Add(a_i^l)$ ,  $Del(a_i^l)$  and  $Con(a_i^l)$  are obtained.

- Replace each constant in  $Pre(a_i^l)$ ,  $Add(a_i^l)$ ,  $Del(a_i^l)$  and  $Con(a_i^l)$  with a unique variable, to form the final action,  $a_i^l$ .

## Methodology

# Learning Algorithm

5. For each set  $A_i^k$ , calculate the Similarity Index,  $SI(A_i^k, Actions_i)$ .
6. If  $Actions_i^{new} = A_i^p$  such that  $SI(A_i^p, Actions_i) > SI(A_i^q, Actions_i)$ ,  $\forall q \neq p$ . Then,  $Partition_{co}^p$  is the final choice for learning.
7.  $\forall a_i^k \in Actions_i^{new}$ , if  $\exists p_{co}^k \in Pre(a_i^k)$  or  $\exists p_{co}^k \in Add(a_i^k)$  or  $\exists p_{co}^k \in Con(a_i^k)$ , such that
  - a.  $p_{co}^k \notin KB_i$ , then let  $p_i^k = p_{co}^k$  and  $Pred_i^{new} = Pred_i^{new} \cup p_i^k$   
Formulate a translator  $t_i^k$  that represents the mapping
$$p_i^k \xleftrightarrow{t_i^k} p_{co}^k$$
  - b. If  $p_{co}^k = p_i^k \in KB_i$ , and  $\nexists t_i^k \in Trans_i$  such that  $p_i^k \xleftrightarrow{t_i^k} p_{co}^k$   
then create the translator,  $t_i^k$ .Let  $Trans_i^{new} = Trans_i^{new} \cup t_i^k$ .

Methodology  
Learning Algorithm

8.  $\forall a_i^k \in Actions_i^{new}$ ,

1. If  $a_i^k \notin Actions_i$ , generate a new name that is the concatenation of the action names in the common ontology. The parameters of  $a_i^k$  consist of the list of all the variables that are a part of the action definition of  $a_i^k$ . Form the translator  $t_i^k$  which represents the mapping

$$a_i^k \xleftrightarrow{t_i^k} \langle A_{co}^{p-k}, O_{co}^{p-k} \rangle$$

If  $a_i^k = a_i^l \in Actions_i$ ,  $l \neq k$  and  $\nexists t_i^l \in Trans_i$  such that

$$a_i^k \xleftrightarrow{t_i^l} \langle A_{co}^{p-k}, O_{co}^{p-k} \rangle$$

then formulate the translator.

$$\text{Let } Trans_i^{new} = Trans_i^{new} \cup t_i^l$$

9. Update  $KB_i$  with the new information

$$Pred_i = Pred_i \cup Pred_i^{new}$$

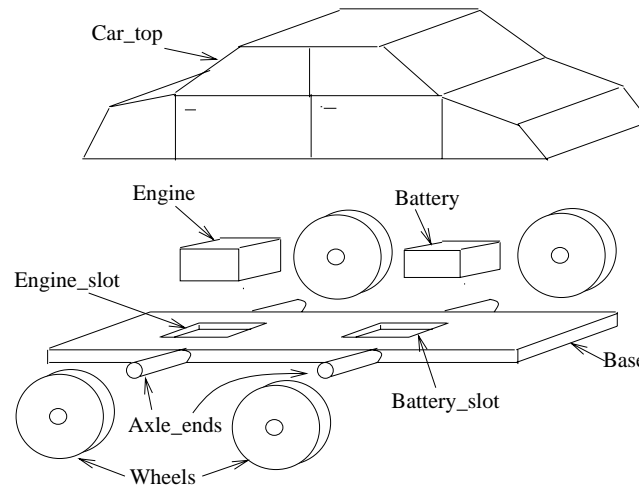
$$Actions_i = Actions_i \cup Actions_i^{new}$$

$$Trans_i = Trans_i \cup Trans_i^{new}$$



# Example

## Planner<sub>3</sub> – Toy Car Assembly



$I_3 = \text{Clear}_3(\text{Axle\_end1}), \text{Clear}_3(\text{Axle\_end2}), \text{Clear}_3(\text{Axle\_end3}), \text{Clear}_3(\text{Axle\_end4}),$   
 $\text{Clear}_3(\text{Wheel1}), \text{Clear}_3(\text{Wheel2}), \text{Clear}_3(\text{Wheel3}), \text{Clear}_3(\text{Wheel4}), \text{Clear}_3(\text{Eng}),$   
 $\text{Clear}_3(\text{Batt}), \text{Clear}_3(\text{Eng\_slot}), \text{Clear}_3(\text{Batt\_slot}), \text{Clear}_3(\text{Top}), \text{Clear}_3(\text{Base})$

$G_3 = \text{Car}_2$

$C_3 = \text{Wheel}_3(\text{Wheel1}), \text{Wheel}_3(\text{Wheel2}), \text{Wheel}_3(\text{Wheel3}), \text{Wheel}_3(\text{Wheel4}), \text{Car\_top}_3(\text{Top}),$   
 $\text{Car\_base}_3(\text{Base}), \text{Axle\_end}_3(\text{Axle\_end1}), \text{Axle\_end}_3(\text{Axle\_end2}),$   
 $\text{Axle\_end}_3(\text{Axle\_end3}), \text{Axle\_end}_3(\text{Axle\_end4}), \text{Engine}_3(\text{Eng}), \text{Engine\_slot}_3(\text{Eng\_slot}),$   
 $\text{Battery}_3(\text{Batt}), \text{Battery\_slot}_3(\text{Batt\_Slot})$

Example  
**Planner<sub>3</sub> – Action Descriptions**

Action	Pre	Add	Del	Con
Fix_together <sub>3</sub> (?x,?y)	Clear <sub>3</sub> (?x) Clear <sub>3</sub> (?y)	On <sub>3</sub> (?x,?y) Attached <sub>3</sub> (?x,?y)	Clear(?y)	
Insert_wheel <sub>3</sub> (?y,?x)	Clear <sub>3</sub> (?x), Clear <sub>3</sub> (?y)	Inserted_wheel <sub>3</sub> (?y,?x)	Clear <sub>3</sub> (?y)	Wheel <sub>3</sub> (?x), Axle_end <sub>3</sub> (?y)
Base_assembly <sub>3</sub> (?bs,?w1,?w2,?w3, ?w4,?ae1,?ae2, ?ae3,?ae4)	Inserted_wheel <sub>3</sub> (?ae1,?w1) Inserted_wheel <sub>3</sub> (?ae2,?w2) Inserted_wheel <sub>3</sub> (?ae3,?w3) Inserted_wheel <sub>3</sub> (?ae4,?w4)	Assembled_base_car <sub>1</sub> <sub>3</sub>		Wheel <sub>3</sub> (?w1), Wheel <sub>3</sub> (?w2) Wheel <sub>3</sub> (?w3), Wheel <sub>3</sub> (?w4) Axle_end <sub>3</sub> (?ae1), Axle_end <sub>3</sub> (?ae2) Axle_end <sub>3</sub> (?ae3) Axle_end <sub>3</sub> (?ae4) Car_base <sub>3</sub> (?bs)
Body_assembly <sub>3</sub> (?tp,?bs)	Fastened <sub>3</sub> (?tp,?bs) On <sub>3</sub> (?tp,?bs) Assembled_base_3	Assembled_body <sub>3</sub>		Car_top <sub>3</sub> (?tp) Car_base <sub>3</sub>
Make_car <sub>1</sub> <sub>3</sub>	Assembled_base_car <sub>1</sub> <sub>3</sub> Assembled_body <sub>3</sub>	Car <sub>1</sub> <sub>3</sub>		
Make_car <sub>2</sub> <sub>3</sub>	Assembled_base_car <sub>2</sub> <sub>3</sub> Assembled_body <sub>3</sub>	Car <sub>2</sub> <sub>3</sub>		

# Example Planner<sub>3</sub> – Mappings

Action Mappings in KB<sub>3</sub>

Planner <sub>3</sub>	Common Ontology
Fix_together <sub>3</sub> (?x, ?y)	Pickup <sub>co</sub> (?x) > Align <sub>co</sub> (?x,?y) > Place <sub>co</sub> {co}(?x,?y) > Attach_on <sub>co</sub> (?x,?y)
Insert_wheel <sub>3</sub> (?x, ?y)	Pickup <sub>co</sub> {co}(?x) > Align <sub>co</sub> (?x,?y) > Insert_wheel <sub>co</sub> (?x,?y)
Base_assembly_car <sub>1</sub> (?bs)	Wheel_assembly <sub>co</sub> > Base_assembly <sub>co</sub> (?bs,Car1)
Body_assembly <sub>3</sub> (?cr,?tp,?bs)	Body_assembly <sub>co</sub> (?cr,?tp,?bs)
Make_car <sub>1</sub>	Assemble <sub>co</sub> (Car1)
Make_car <sub>2</sub>	Assemble <sub>co</sub> (Car2)

Domain Truth Table of Planner<sub>3</sub>

Always True	Always False
Handempty <sub>co</sub>	Holding <sub>co</sub>

Predicate Mappings in KB<sub>3</sub>

Planner <sub>3</sub>	Common Ontology
On <sub>3</sub> (?x,?y)	On <sub>co</sub> (?x,?y)
Inserted_wheel <sub>3</sub> (?x,?y)	In_wheel <sub>co</sub> (?x,?y)
Clear <sub>3</sub> (?x)	Clear <sub>co</sub> (?x)
Fastened <sub>3</sub> (?x,?y)	Attached <sub>co</sub> (?x,?y)
Connected <sub>3</sub> (?x,?y)	Wired <sub>co</sub> (?x,?y)
Wheel <sub>3</sub> (?x)	Wheel <sub>co</sub> (?x)
Axle_end <sub>3</sub> (?x)	Axle_end <sub>co</sub> (?x)
Engine <sub>3</sub> (?x)	Engine <sub>co</sub> (?x)
Battery <sub>3</sub> (?x)	Battery <sub>co</sub> (?x)
Engine_slot <sub>3</sub> (?x)	Engine_slot <sub>co</sub> (?x)
Battery_slot <sub>3</sub> (?x)	Battery_slot <sub>co</sub> (?x)
Car_top <sub>3</sub> (?x)	Top <sub>co</sub> (?x)
Car_base <sub>3</sub> (?x)	Base <sub>co</sub> (?x)
Car <sub>3</sub> (?x)	Car <sub>co</sub> (?x)
Assembled_eng_batt <sub>3</sub>	Assembled_eng_batt <sub>co</sub>
Assembled_base_car <sub>1</sub>	Assembled_base <sub>co</sub> (Car1)
Assembled_base_car <sub>2</sub>	Assembled_base <sub>co</sub> (Car2)
Assembled_body_3	Assembled_body <sub>co</sub>
Car <sub>1</sub>	Complete <sub>co</sub> (Car1)
Car <sub>2</sub>	Complete <sub>co</sub> (Car2)

## Example Planner<sub>3</sub> - Query

Query<sub>3</sub>

$I_3 = \text{Clear}_3(\text{Axle\_end1}), \text{Clear}_3(\text{Axle\_end2}), \text{Clear}_3(\text{Axle\_end3}), \text{Clear}_3(\text{Axle\_end4}),$   
 $\text{Clear}_3(\text{Wheel1}), \text{Clear}_3(\text{Wheel2}), \text{Clear}_3(\text{Wheel3}), \text{Clear}_3(\text{Wheel4}), \text{Clear}_3(\text{Eng}),$   
 $\text{Clear}_3(\text{Batt}), \text{Clear}_3(\text{Eng\_slot}), \text{Clear}_3(\text{Batt\_slot}), \text{Clear}_3(\text{Top}), \text{Clear}_3(\text{Base}),$

$G_3 = \text{Assembled\_base\_car2}_3$

$C_3 = \text{Wheel}_3(\text{Wheel1}), \text{Wheel}_3(\text{Wheel2}), \text{Wheel}_3(\text{Wheel3}), \text{Wheel}_3(\text{Wheel4}), \text{Car\_top}_3(\text{Top}),$   
 $\text{Car\_base}_3(\text{Base}), \text{Axle\_end}_3(\text{Axle\_end1}), \text{Axle\_end}_3(\text{Axle\_end2}),$   
 $\text{Axle\_end}_3(\text{Axle\_end3}), \text{Axle\_end}_3(\text{Axle\_end4}), \text{Engine}_3(\text{Eng}), \text{Engine\_slot}_3(\text{Eng\_slot}),$   
 $\text{Battery}_3(\text{Batt}), \text{Battery\_slot}_3(\text{Batt\_Slot})$

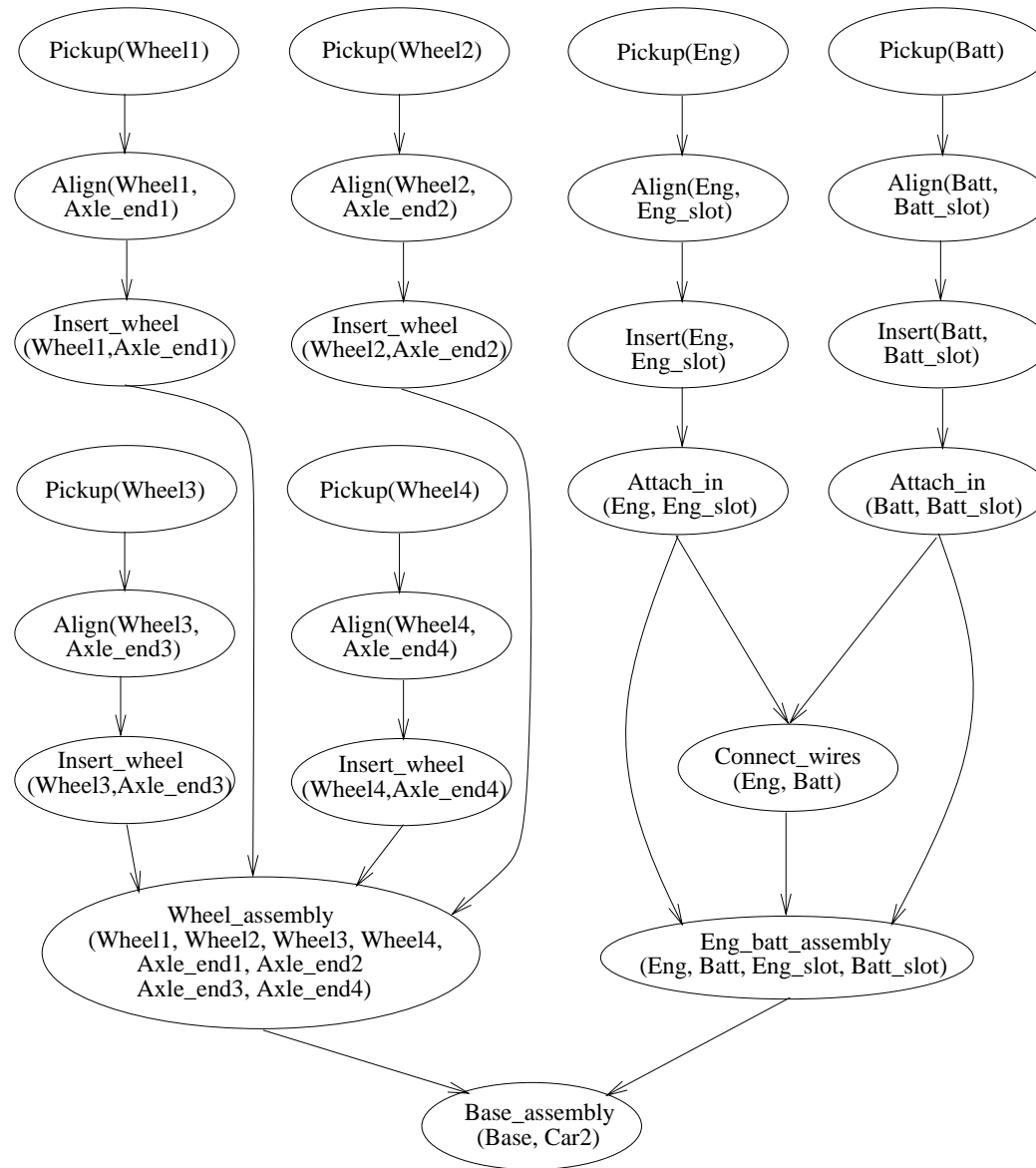
Query<sub>co</sub>

$I_{co} = \text{Clear}_{co}(\text{Axle\_end1}), \text{Clear}_{co}(\text{Axle\_end2}), \text{Clear}_{co}(\text{Axle\_end3}), \text{Clear}_{co}(\text{Axle\_end4}),$   
 $\text{Clear}_{co}(\text{Wheel1}), \text{Clear}_{co}(\text{Wheel2}), \text{Clear}_{co}(\text{Wheel3}), \text{Clear}_{co}(\text{Wheel4}), \text{Clear}_{co}(\text{Eng}),$   
 $\text{Clear}_{co}(\text{Batt}), \text{Clear}_{co}(\text{Eng\_slot}), \text{Clear}_{co}(\text{Batt\_slot}), \text{Clear}_{co}(\text{Top}), \text{Clear}_{co}\}(\text{Base})$

$G_{co} = \text{Assembled\_base}_{co}(\text{Car2})$

$C_{co} = \text{Wheel}_{co}(\text{Wheel1}), \text{Wheel}_{co}(\text{Wheel2}), \text{Wheel}_{co}(\text{Wheel3}), \text{Wheel}_{co}(\text{Wheel4}),$   
 $\text{Top}_{co}(\text{Top}), \text{Base}_{co}(\text{Base}), \text{Axle\_end}_{co}(\text{Axle\_end1}), \text{Axle\_end}_{co}(\text{Axle\_end2}),$   
 $\text{Axle\_end}_{co}(\text{Axle\_end3}), \text{Axle\_end}_{co}(\text{Axle\_end4}), \text{Engine}_{co}(\text{Eng}),$   
 $\text{Engine\_slot}_{co}(\text{Eng\_slot}), \text{Battery}_{co}(\text{Batt}), \text{Battery\_slot}_{co}(\text{Batt\_Slot}), \text{Handempty}_{co}$

Example  
Common  
Ontology –  
Solution  
Plan



## Example

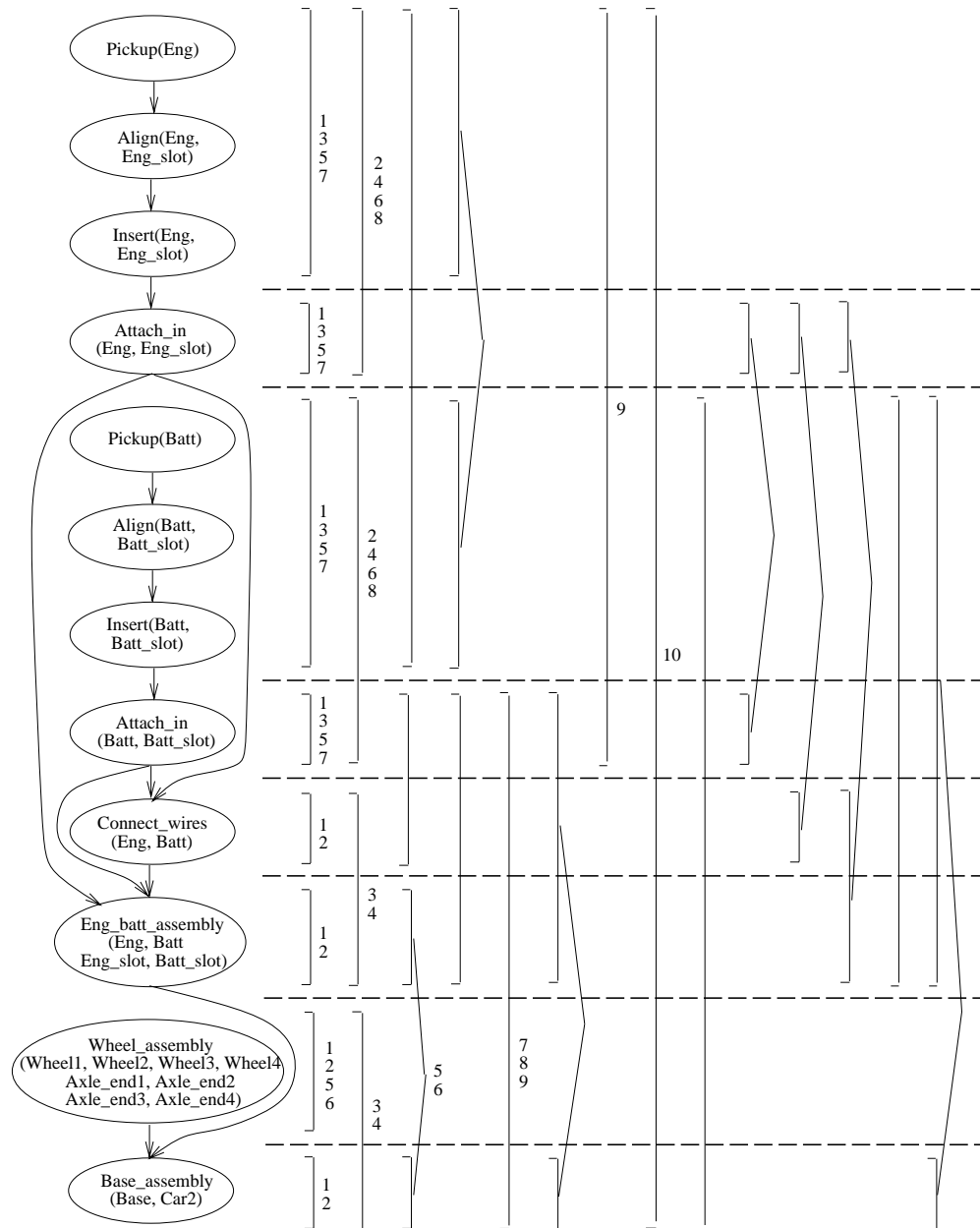
# Common Ontology – Solution Plan

$A_{co} = a_{co}^1 = \text{Pickup}_{co}(\text{Wheel1}),$   
 $a_{co}^2 = \text{Align}_{co}(\text{Wheel1}, \text{Axle\_end1}),$   
 $a_{co}^3 = \text{Insert\_wheel}_{co}(\text{Wheel1}, \text{Axle\_end1}),$   
 $a_{co}^4 = \text{Pickup}_{co}(\text{Wheel2}),$   
 $a_{co}^5 = \text{Align}_{co}(\text{Wheel}, \text{Axle\_end2}),$   
 $a_{co}^6 = \text{Insert\_wheel}_{co}(\text{Wheel2}, \text{Axle\_end2}),$   
 $a_{co}^7 = \text{Pickup}_{co}(\text{Wheel3}),$   
 $a_{co}^8 = \text{Align}_{co}(\text{Wheel3}, \text{Axle\_end3}),$   
 $a_{co}^9 = \text{Insert\_wheel}_{co}(\text{Wheel3}, \text{Axle\_end3}),$   
 $a_{co}^{10} = \text{Pickup}_{co}(\text{Wheel4}),$   
 $a_{co}^{11} = \text{Align}_{co}(\text{Wheel4}, \text{Axle\_end4}),$   
 $a_{co}^{12} = \text{Insert\_wheel}_{co}(\text{Wheel4}, \text{Axle\_end4}),$   
 $a_{co}^{13} = \text{Wheel\_assembly}(\text{Wheel1}, \text{Wheel2}, \text{Wheel3},$   
 $\text{Wheel4}, \text{Axle\_end1}, \text{Axle\_end2}, \text{Axle\_end3}, \text{Axle\_end4})$

$a_{co}^{14} = \text{Pickup}_{co}(\text{Eng}),$   
 $a_{co}^{15} = \text{Align}_{co}(\text{Eng}, \text{Eng\_slot}),$   
 $a_{co}^{16} = \text{Insert}_{co}(\text{Eng}, \text{Eng\_slot}),$   
 $a_{co}^{17} = \text{Attach\_in}_{co}(\text{Eng}, \text{Eng\_slot}),$   
 $a_{co}^{18} = \text{Pickup}_{co}(\text{Batt}),$   
 $a_{co}^{19} = \text{Align}_{co}(\text{Batt}, \text{Batt\_slot}),$   
 $a_{co}^{20} = \text{Insert}_{co}(\text{Batt}, \text{Batt\_slot}),$   
 $a_{co}^{21} = \text{Attach\_in}_{co}(\text{Batt}, \text{Batt\_slot}),$   
 $a_{co}^{22} = \text{Connect\_wires}_{co}(\text{Eng},$   
 $\text{Batt}, \text{Eng\_slot}, \text{Batt\_slot}),$   
 $a_{co}^{23} = \text{Eng\_batt\_assembly}_{co}(\text{Eng},$   
 $\text{Batt}, \text{Eng\_slot}, \text{Batt\_slot}),$   
 $a_{co}^{24} = \text{Base\_assembly}_{co}(\text{Base}, \text{Car2})$

$O_{co} = \text{before}(a_{co}^1, a_{co}^2), \text{before}(a_{co}^2, a_{co}^3), \text{before}(a_{co}^4, a_{co}^5), \text{before}(a_{co}^7, a_{co}^6), \text{before}(a_{co}^7, a_{co}^8),$   
 $\text{before}(a_{co}^8, a_{co}^9), \text{before}(a_{co}^{10}, a_{co}^{11}), \text{before}(a_{co}^{11}, a_{co}^{12}), \text{before}(a_{co}^3, a_{co}^{13}), \text{before}(a_{co}^6, a_{co}^{13}), \text{before}(a_{co}^9, a_{co}^{13}),$   
 $\text{before}(a_{co}^{12}, a_{co}^{13}), \text{before}(a_{co}^{14}, a_{co}^{15}), \text{before}(a_{co}^{15}, a_{co}^{16}), \text{before}(a_{co}^{16}, a_{co}^{17}), \text{before}(a_{co}^{18}, a_{co}^{19}), \text{before}(a_{co}^{19}, a_{co}^{20}),$   
 $\text{before}(a_{co}^{20}, a_{co}^{21}), \text{before}(a_{co}^{17}, a_{co}^{22}), \text{before}(a_{co}^{21}, a_{co}^{22}), \text{before}(a_{co}^{17}, a_{co}^{23}), \text{before}(a_{co}^{21}, a_{co}^{23}), \text{before}(a_{co}^{22}, a_{co}^{23}),$   
 $\text{before}(a_{co}^{13}, a_{co}^{24}), \text{before}(a_{co}^{23}, a_{co}^{24})$

# Example Solution Plan - Partitions



## Example

# Solution Plan - Partition<sub>co</sub><sup>1</sup>

$$A_{co}^{1-1} = \{a_{co}^1, a_{co}^2, a_{co}^3\}$$

$$A_{co}^{1-2} = \{a_{co}^4, a_{co}^5, a_{co}^6\}$$

$$A_{co}^{1-3} = \{a_{co}^7, a_{co}^8, a_{co}^9\}$$

$$A_{co}^{1-4} = \{a_{co}^{10}, a_{co}^{11}, a_{co}^{12}\}$$

$$A_{co}^{1-5} = \{a_{co}^{14}, a_{co}^{15}, a_{co}^{16}\}$$

$$A_{co}^{1-6} = \{a_{co}^{17}\}$$

$$A_{co}^{1-7} = \{a_{co}^{18}, a_{co}^{19}, a_{co}^{20}\}$$

$$A_{co}^{1-8} = \{a_{co}^{21}\}$$

$$A_{co}^{1-9} = \{a_{co}^{22}\}$$

$$A_{co}^{1-10} = \{a_{co}^{23}\}$$

$$A_{co}^{1-11} = \{a_{co}^{13}\}$$

$$A_{co}^{1-12} = \{a_{co}^{24}\}$$

$$O_{co}^{1-1} = \{(a_{co}^1 > a_{co}^2), (a_{co}^2 > a_{co}^3)\},$$

$$O_{co}^{1-2} = \{(a_{co}^4 > a_{co}^5), (a_{co}^5 > a_{co}^6)\},$$

$$O_{co}^{1-3} = \{(a_{co}^7 > a_{co}^8), (a_{co}^8 > a_{co}^9)\},$$

$$O_{co}^{1-4} = \{(a_{co}^{10} > a_{co}^{11}), (a_{co}^{11} > a_{co}^{12})\},$$

$$O_{co}^{1-5} = \{(a_{co}^{14} > a_{co}^{15}), (a_{co}^{15} > a_{co}^{16})\},$$

$$O_{co}^{1-6} = \{ \}$$

$$O_{co}^{1-7} = \{(a_{co}^{18} > a_{co}^{19}), (a_{co}^{19} > a_{co}^{20})\},$$

$$O_{co}^{1-8} = \{ \}$$

$$O_{co}^{1-9} = \{ \}$$

$$O_{co}^{1-10} = \{ \}$$

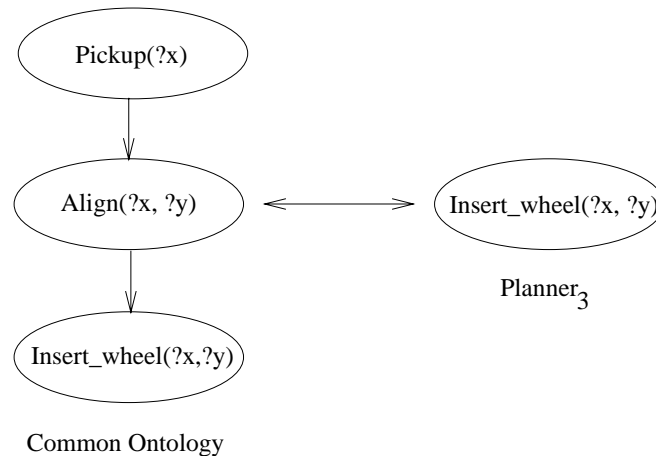
$$O_{co}^{1-11} = \{ \}$$

$$O_{co}^{1-12} = \{ \}$$

$$O_{co}^{1-13} = \{(a_{co}^{16} > a_{co}^{17}), (a_{co}^{17} > a_{co}^{22}), (a_{co}^{17} > a_{co}^{23}), (a_{co}^{20} > a_{co}^{21}), (a_{co}^{21} > a_{co}^{22}), (a_{co}^{22} > a_{co}^{23}), (a_{co}^{22} > a_{co}^{23}), (a_{co}^{23} > a_{co}^{24}), (a_{co}^{13} > a_{co}^{24})\}$$



Example  
Solution Plan - Partition<sub>co</sub><sup>1</sup>



- Groups

$\langle A_{co}^{1-1}, O_{co}^{1-1} \rangle, \langle A_{co}^{1-2}, O_{co}^{1-2} \rangle,$   
 $\langle A_{co}^{1-3}, O_{co}^{1-3} \rangle, \langle A_{co}^{1-4}, O_{co}^{1-4} \rangle$

all translate to the action

$Insert\_wheel_3(?x,?y)$

Example  
Partition<sub>co</sub><sup>1</sup> – New Actions

- Group  $\langle A_{co}^{1-5}, O_{co}^{1-5} \rangle$  cannot be translated
- It has the following Preconditions, Add list, Delete List & Constraints
  - Pre  $(\langle A_{co}^{1-5}, O_{co}^{1-5} \rangle) = \text{Clear}_{co}(\text{Eng}), \text{Clear}_{co}(\text{Eng\_slot})$
  - Add  $(\langle A_{co}^{1-5}, O_{co}^{1-5} \rangle) = \text{In}_{co}(\text{Eng}, \text{Eng\_slot})$
  - Del  $(\langle A_{co}^{1-5}, O_{co}^{1-5} \rangle) = \text{Clear}_{co}(\text{Eng\_slot})$
  - Con  $(\langle A_{co}^{1-5}, O_{co}^{1-5} \rangle) = --$
- The new action this would form is
  - $a_3^1(?x, ?y)$
  - Pre  $(a_3^1) = \text{Clear}_3(?x), \text{Clear}_3(?y)$
  - Add  $(a_3^1) = \mathbf{In}_{co}(?x, ?y)$
  - Del  $(a_3^1) = \text{Clear}_3(?y)$
  - Con  $(a_3^1) = -$
- The similarity index is  $\text{SI}(a_3^1, \text{Fix\_together}_3) = 0.4$
- The element  $\langle A_{co}^{1-7}, O_{co}^{1-7} \rangle$  forms a new action,  $a_3^3$ , that is equal to  $a_3^1$ .  
 Therefore,  $a_3^3 = a_3^1$  and  $\text{SI}(a_3^3, \text{Fix\_together}_3) = 0.4$

## Example

### Partition<sub>co</sub><sup>1</sup> – New Actions

- Similarly,  $\langle A_{co}^{1-6}, O_{co}^{1-6} \rangle$  and  $\langle A_{co}^{1-8}, O_{co}^{1-8} \rangle$  form actions  $a_3^2$  and  $a_3^4$  which are equal and their similarity indices are

$$SI(a_3^2, \text{Fix\_together}_3) = 0.2$$

$$SI(a_3^4, \text{Fix\_together}_3) = 0.2$$

- Finally,  $\langle A_{co}^{1-9}, O_{co}^{1-9} \rangle$ ,  $\langle A_{co}^{1-10}, O_{co}^{1-10} \rangle$ ,  $\langle A_{co}^{1-11}, O_{co}^{1-11} \rangle$  and  $\langle A_{co}^{1-12}, O_{co}^{1-12} \rangle$  form the new actions  $a_3^5(?w, ?x, ?y, ?z)$ ,  $a_3^6(?en, ?bt, ?es, ?bs)$ ,  $a_3^7(?en, ?bt, ?es, ?bs)$  and  $a_3^8(?w, ?x, ?y, ?z)$  whose similarity indices are as below.

$$SI(a_3^5, \text{Fix\_together}_3) = 0.125$$

$$SI(a_3^6, \text{Body\_assembly}_3) = 0.067$$

$$SI(a_3^7, \text{Base\_assembly}_3) = 0.75$$

$$SI(a_3^8, \text{Base\_assembly}_3) = 0.105$$

- The similarity index of the entire set is

$$SI(A_3^1, \text{Actions}_3) = 0.281$$

## Example

# Solution Plan – Calculation Results

- Below are a few of the highest similarity indices for the remaining partitions.

$$SI(A_3^2, \text{Actions}_3) = 0.374$$

$$SI(A_3^3, \text{Actions}_3) = 0.348$$

$$SI(A_3^4, \text{Actions}_3) = 0.523$$

$$SI(A_3^5, \text{Actions}_3) = 0.344$$

$$SI(A_3^6, \text{Actions}_3) = 0.515$$

$$SI(A_3^7, \text{Actions}_3) = 0.348$$

$$\mathbf{SI(A_3^8, \text{Actions}_3) = 0.579}$$

$$SI(A_3^9, \text{Actions}_3) = 0.436$$

$$SI(A_3^{10}, \text{Actions}_3) = 0.467$$

- The set  $A_3^8$  is most similar to the existing knowledge in Planner<sub>3</sub>.

Example  
Planner<sub>3</sub> - New Actions

$A_3^8 = \{a_3^1, a_3^2, a_3^3\}$ , contains 3 new actions described as follows.

$a_3^1(?x,?y) = a_3^2(?x,?y)$

$Pre(a_3^1) = Pre(a_3^2) = Clear_3(?x), Clear_3(?y)$

$Add(a_3^1) = Add(a_3^2) = \mathbf{In_{co}}(?x,?y), Fastened_3(?x,?y)$

$Del(a_3^1) = Del(a_3^2) = Clear_3(?y)$

$Con(a_3^1) = Con(a_3^2) = -$

$a_3^3(?en,?bt,?es,?bs,?bs1,?cr)$

$Pre(a_3^3) = Inserted\_wheel_3(?w1,?ae1),$

$Inserted\_wheel_3(?w2,?ae2), Inserted\_wheel_3(?w3,?ae3),$

$Inserted\_wheel_3(?w4,?ae4), Fastened_3(?en,?es),$

$Fastened_3(?bt,?bs), \mathbf{In_{co}}(?en,?es), \mathbf{In_{co}}(?bt,?bs),$

$Wheel_3(?w1), Wheel_3(?w2),$

$Add(a_3^3) = Connected_3(?en,?bt), Assembled\_base\_car2_3$

$Del(a_3^3) = --$

$Con(a_3^3) = Wheel_3(?w3), Wheel_3(?w4), Axle\_end_3(?ae1),$

$Axle\_end_3(?ae2), Axle\_end_3(?ae3), Axle\_end_3(?ae4),$

$Engine_3(?en), Battery_3(?bt), Engine\_slot_3(?es),$

$Battery\_slot_3(?bt), Base_3(?bs1), \mathbf{Car_{co}}(\mathbf{Car2})$

Example

Planner<sub>3</sub> – New Mappings

<b>Planner<sub>3</sub></b>	<b>Common Ontology</b>
In <sub>3</sub> (?x,?y)	In <sub>co</sub> (x,?y)
Car <sub>3</sub> (?x)	Car <sub>co</sub> (?x)
Pickup_align_insert_attach_in <sub>3</sub> (?x, ?y)	Pickup <sub>co</sub> (?x) > Align <sub>co</sub> (?x,?y) > Insert <sub>co</sub> (?x,?y) > Attach_in <sub>co</sub> (?x,?y)
Connect_wires_eng_batt_assembly_wheel_ assembly_base_assembly <sub>3</sub> (?w1,?w2,?w3,?w4,?ae1,?ae2, ?ae3,?ae4,?en,?bt,?es,?bs,?bs1,?cr)	Connect_wires <sub>co</sub> (?en,?bt) > Eng_batt_assembly <sub>co</sub> (?en,?bt,?es,?bs) > Wheel_assembly <sub>co</sub> (?w1,?w2,?w3,?w4, ?ae1,?ae2,?ae3,?ae4) > Base_assembly <sub>co</sub> (?bs1,?cr)

Example  
Planner<sub>3</sub> - Final  
Solution

Plan<sub>3</sub>

A<sub>3</sub> =

a<sub>3</sub><sup>1</sup> = Insert\_wheel<sub>3</sub>(Wheel1, Axle\_end1),

a<sub>3</sub><sup>2</sup> = Insert\_wheel<sub>3</sub>(Wheel2, Axle\_end2),

a<sub>3</sub><sup>3</sup> = Insert\_wheel<sub>3</sub>(Wheel3, Axle\_end3),

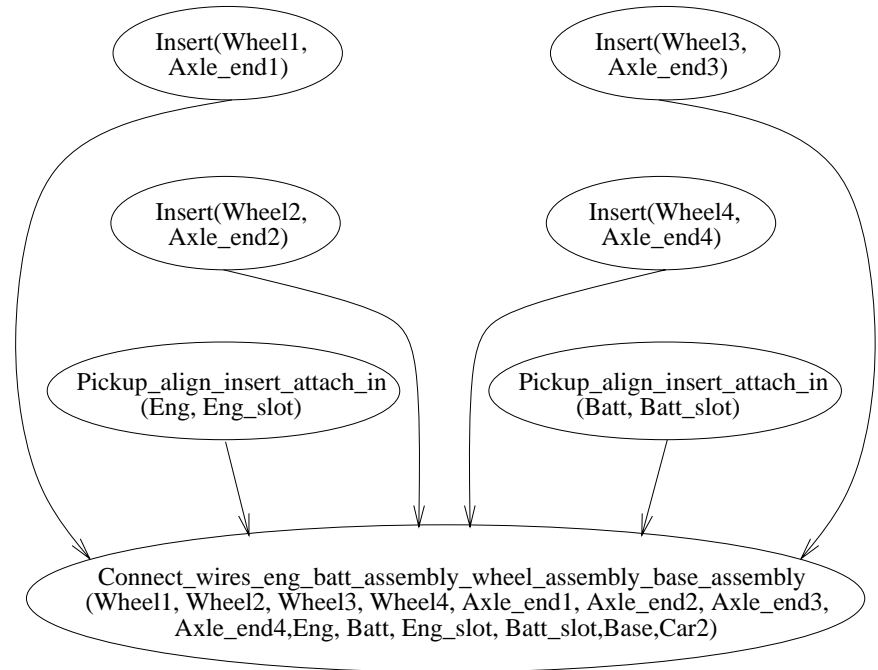
a<sub>3</sub><sup>4</sup> = Insert\_wheel<sub>3</sub>(Wheel4, Axle\_end4),

a<sub>3</sub><sup>5</sup> = Pickup\_align\_insert\_attach\_in<sub>3</sub>(Eng,Eng\_slot),

a<sub>3</sub><sup>6</sup> = Pickup\_align\_insert\_attach\_in<sub>3</sub>(Batt,Batt\_slot),

a<sub>3</sub><sup>7</sup> = Connect\_wires\_eng\_batt\_assembly\_wheel\_assembly\_base\_assembly  
 assembly\_base\_assembly<sub>3</sub>(Wheel1, Wheel2, Wheel3, Wheel4,  
 Axle\_end1, Axle\_end2, Axle\_end3, Axle\_end4, Eng, Batt,  
 Eng\_slot, Batt\_slot, Base, Car2)

O<sub>3</sub> = before(a<sub>3</sub><sup>1</sup>, a<sub>3</sub><sup>7</sup>), before(a<sub>3</sub><sup>2</sup>, a<sub>3</sub><sup>7</sup>), before(a<sub>3</sub><sup>3</sup>, a<sub>3</sub><sup>7</sup>), before(a<sub>3</sub><sup>4</sup>, a<sub>3</sub><sup>7</sup>),  
 before(a<sub>3</sub><sup>5</sup>, a<sub>3</sub><sup>7</sup>), before(a<sub>3</sub><sup>6</sup>, a<sub>3</sub><sup>7</sup>)



## Related Work

Knowledge Interchange Interface - A formal framework for knowledge sharing between planners.

- Given  $\text{Plan}_{\text{co}}$ , the KII learns new knowledge from it as follows.
  - If action  $a_{\text{co}}^k$  contains predicates that are always true or false, it is combined with one or more actions to eliminate these predicates. The resulting composite action is added to  $\text{Planner}_i$ .
  - All other actions are added without any change to  $\text{Planner}_i$
  - All new predicates in the actions are added to  $\text{Pred}_i$ .
  - Translators are formulated for the actions and predicates and added to  $\text{KB}_i$ .
- Drawbacks
  - A subplan in  $\text{Plan}_{\text{co}}$  that have an equivalent action in  $\text{Planner}_i$ , but no translator get mapped to new actions, causing duplication of knowledge in  $\text{Planner}_i$ .
  - Does not handle combinations of subplans in a flexible manner.
  - Adds the same knowledge to planners, regardless of the level of abstraction.



## Related Work

Learning through Exploration and Experimentation - improve the models for planning by using failure-driven experimentation with the environment

- Construction by direct analogy - creates new operators based on operators that are already defined in the system. This is done by direct analogy through the types of objects that the operators are applied to.
- Creation of micro-operators – creates a new operator that performs some subaction of an existing operator.
  - Experimentation is used to determine which preconditions and effects can be discarded in the new operator.
  - A existing action is broken into a sequence of subactions.
- Drawbacks
  - Refines existing knowledge in the system.
  - Does not learn anything new from external sources.

## Related Work

Explanation-Based Learning - generalize a set of given examples into descriptions of concepts.

- Learning composite rules - alters the search space that is explored by combining existing rules to form new, possibly redundant but more efficient, rules. improves the performance of a system without the introduction of new knowledge
- Learning search control knowledge - altering the method in which the search is conducted. Speeds up the search of the concept hypothesis space by formulating heuristics that index the operators in an appropriate order.

Plan Mining - used to discover significant knowledge from a large database of plans such as airline schedules etc.

- Generalization-based divide-and-conquer - used to find high-level, highly regular sequential patterns along more than one dimension.

# Conclusion

- The knowledge acquisition methodology allows a planner in a collection of networked planners to update its domain theory using solution plans that it receives from its peers.
- The information (predicates and actions) contained in a solution plan that cannot be translated is used to extend the knowledge base of the receiving planner.
- The addition of the necessary translators for the new knowledge means that it can be used to solve problems and communicate queries and solution plans in the future.
- The methodology guarantees that this information is correct in the domain of the planner and it is the most similar to the existing knowledge in the planner.